

Composite Higgs models, the LHC, and Lattice

Adam Martin
University of Notre Dame
(amarti41@nd.edu)

Lattice Meets Experiment 2013, BNL, Dec 5th 2013

before ~ July 2012

elementary Higgs (tuned SM, supersymmetry)

composite Higgs

no Higgs

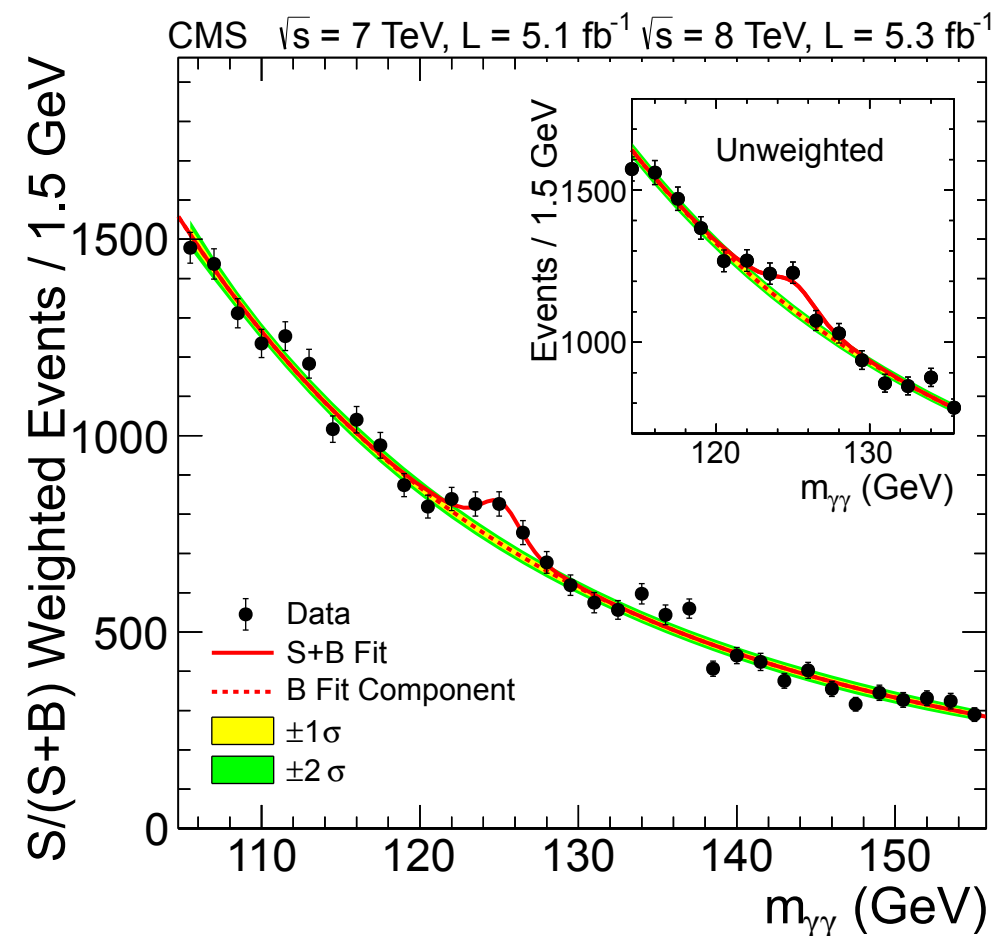
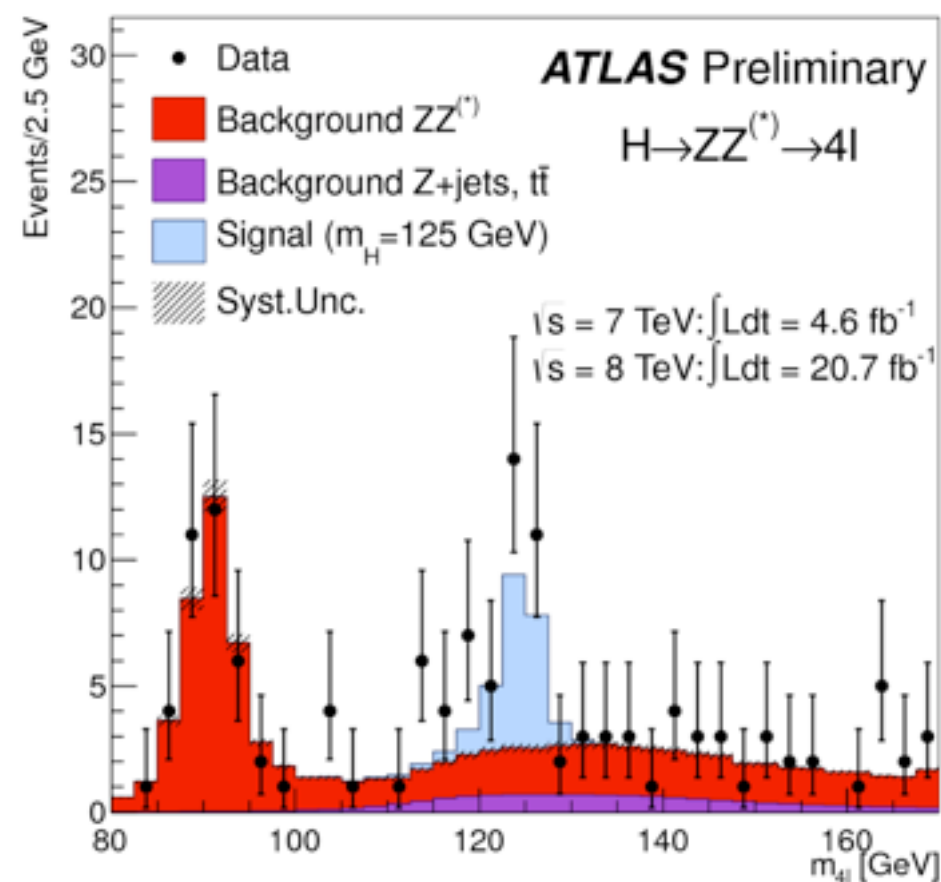
before ~ July 2012

elementary Higgs (tuned SM, supersymmetry)

composite Higgs

no Higgs

Now:



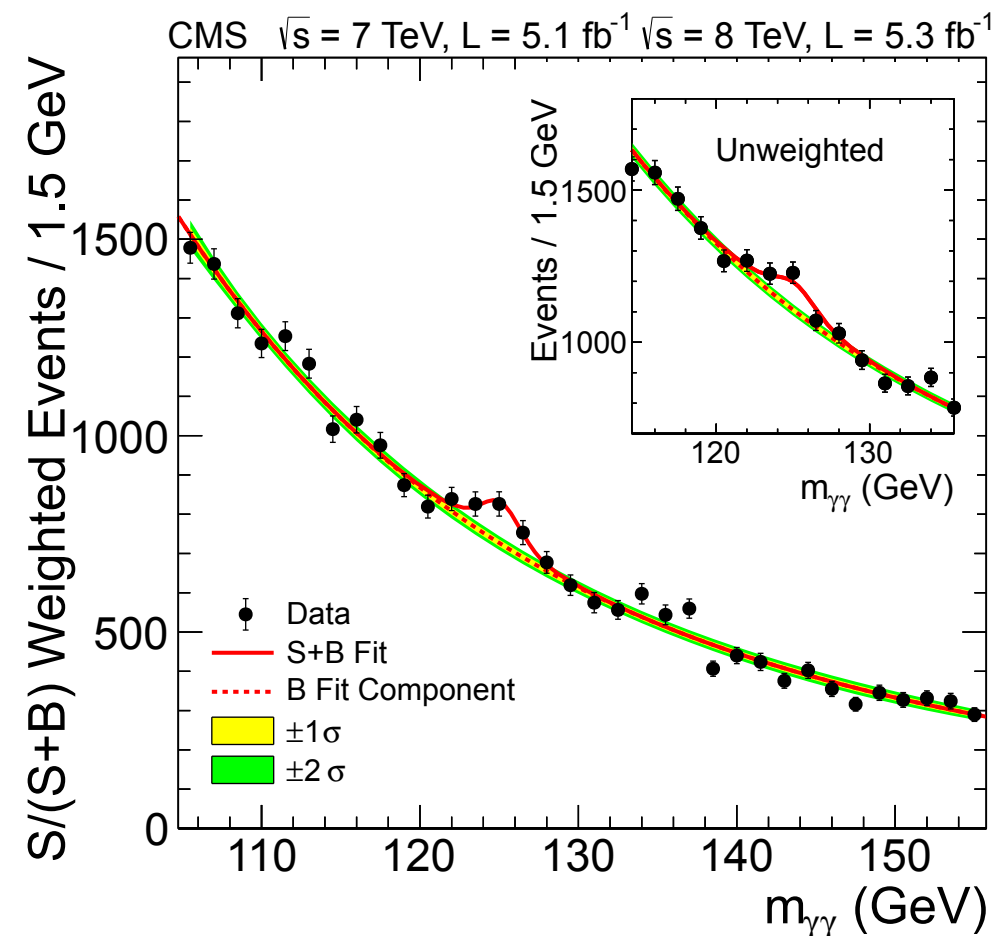
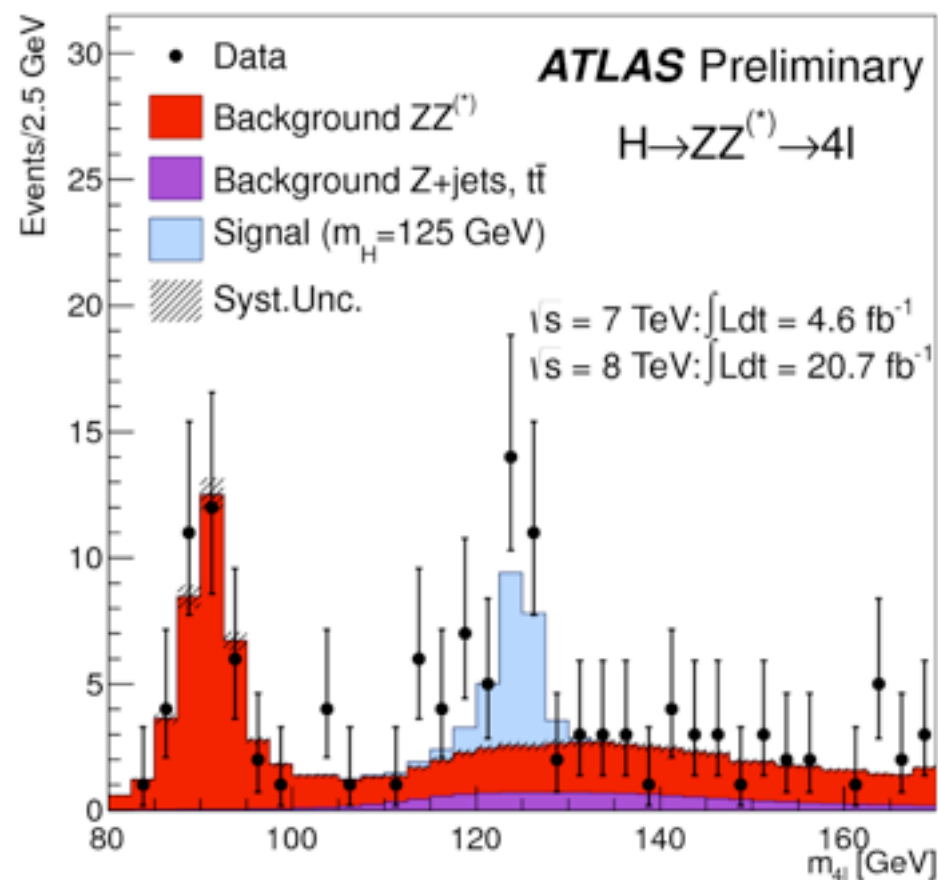
before ~ July 2012

elementary Higgs (tuned SM, supersymmetry)

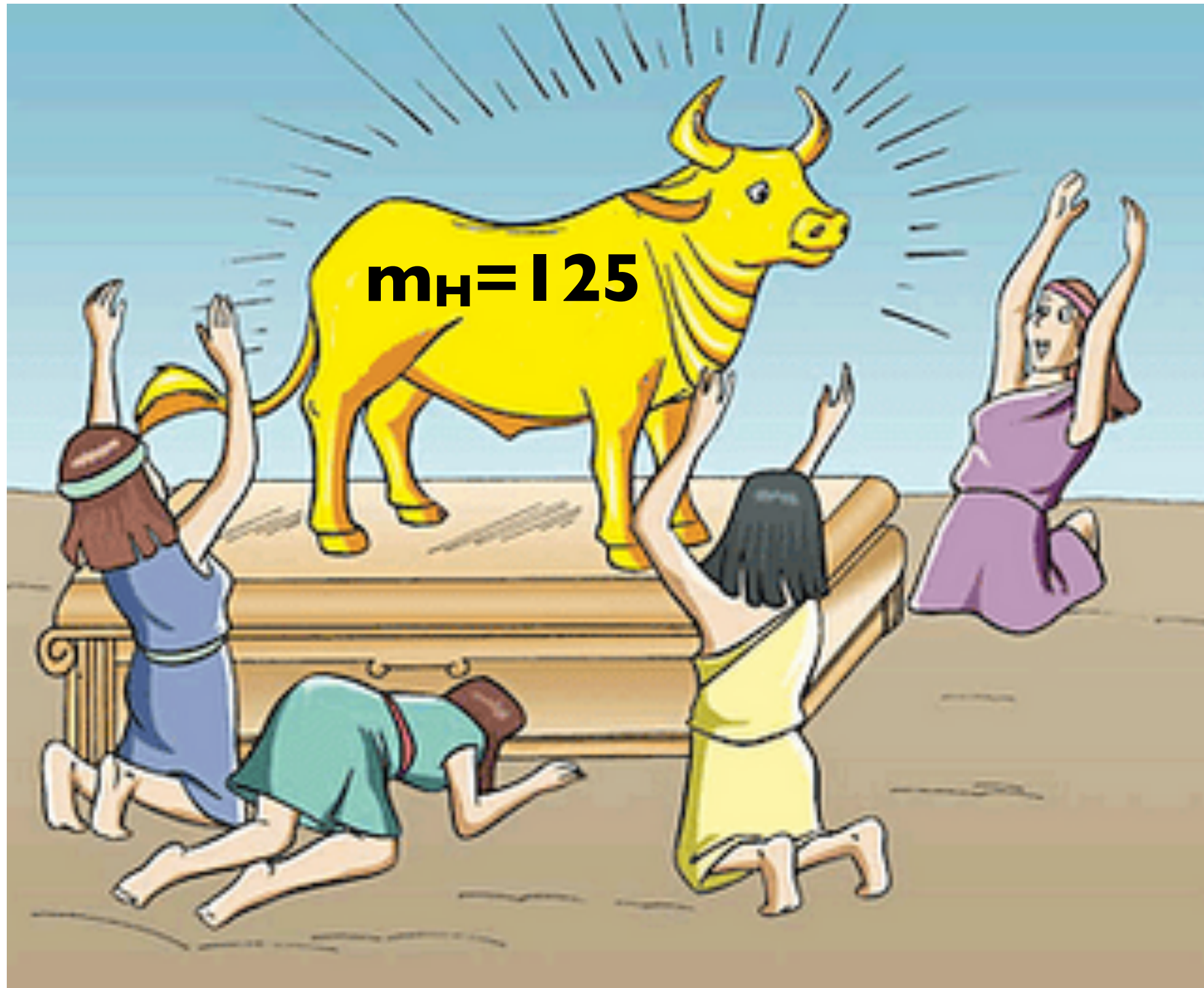
composite Higgs

~~no Higgs~~

Now:



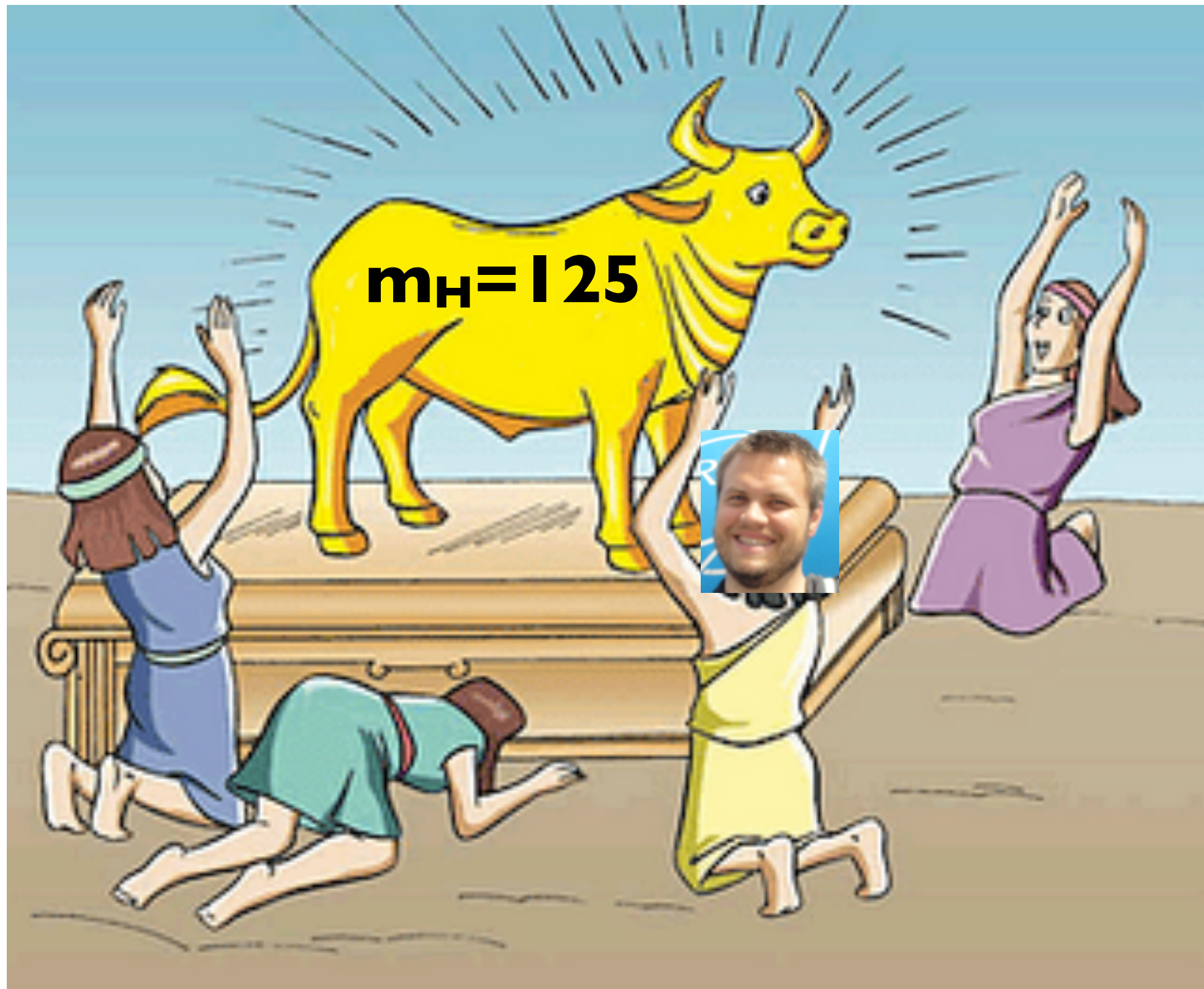
... so lets not get carried away



... so lets not get carried away

from AM, USQCD 5/4/12

now:



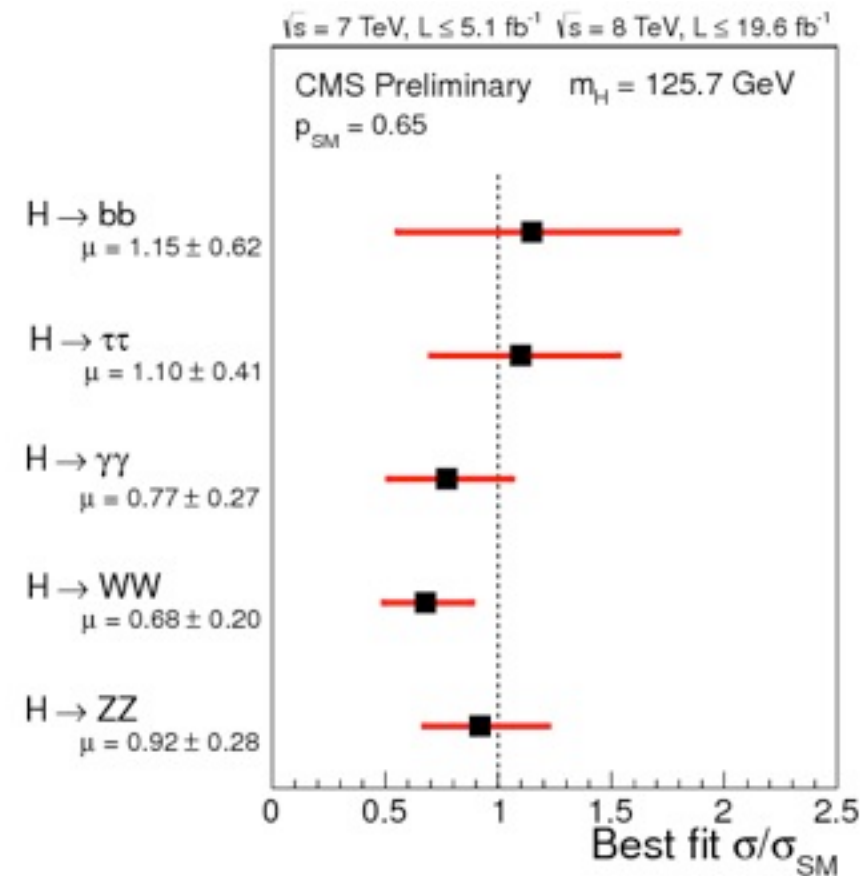
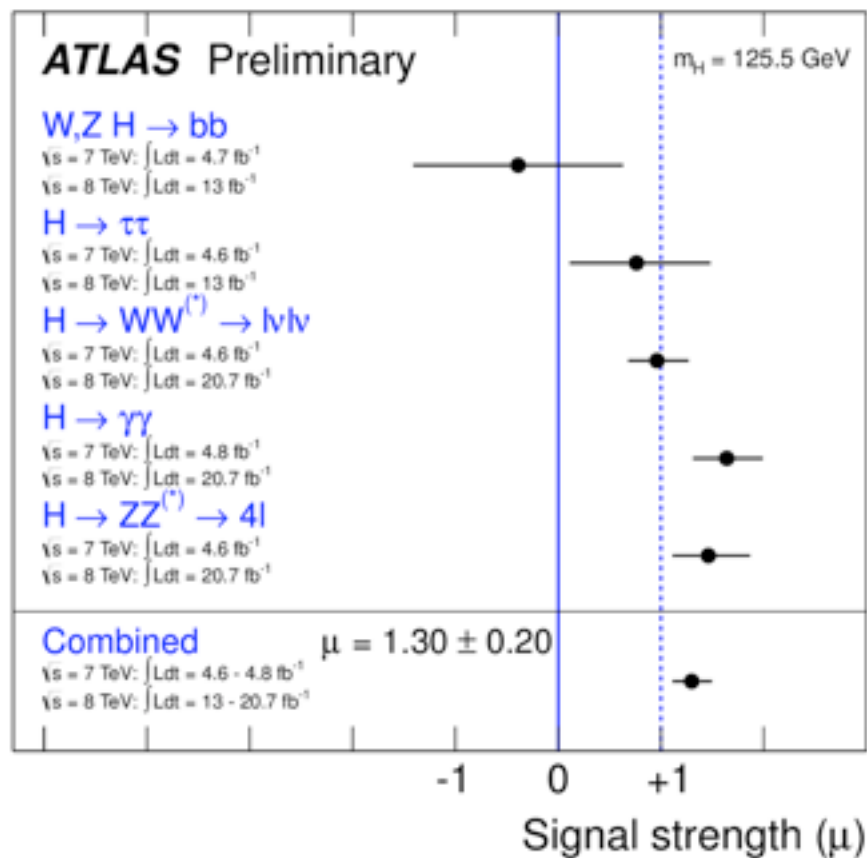
before ~ July 2012

elementary Higgs (tuned SM, supersymmetry)

composite Higgs

~~no Higgs~~

Now:



Composite Higgs

basic idea: Higgs doublet $(2, 1/2)$ is a pNGB .. that is why it is lighter than other new physics

just as $m^2_\pi \ll m^2_\rho$

at some high scale: **f**

$G \rightarrow G' + \text{NGBs}$ from some new strong dynamics

unbroken group G' contains $SU(2) \otimes U(1)$

NGB come in reps. of G' , arrange such that

NGBs contain a doublet H of EWS:

$$\frac{G}{G'} \supset H(2, \frac{1}{2})$$

Composite Higgs

basic idea: Higgs doublet $(2, 1/2)$ is a pNGB .. that is why it is lighter than other new physics

just as $m^2_\pi \ll m^2_\rho$

at some high scale: **f**

$G \rightarrow G' + \text{NGBs}$ from some new strong dynamics
lattice!

unbroken group G' contains $SU(2) \otimes U(1)$

NGB come in reps. of G' , arrange such that

NGBs contain a doublet H of EWS:

$$\frac{G}{G'} \supset H(2, \frac{1}{2})$$

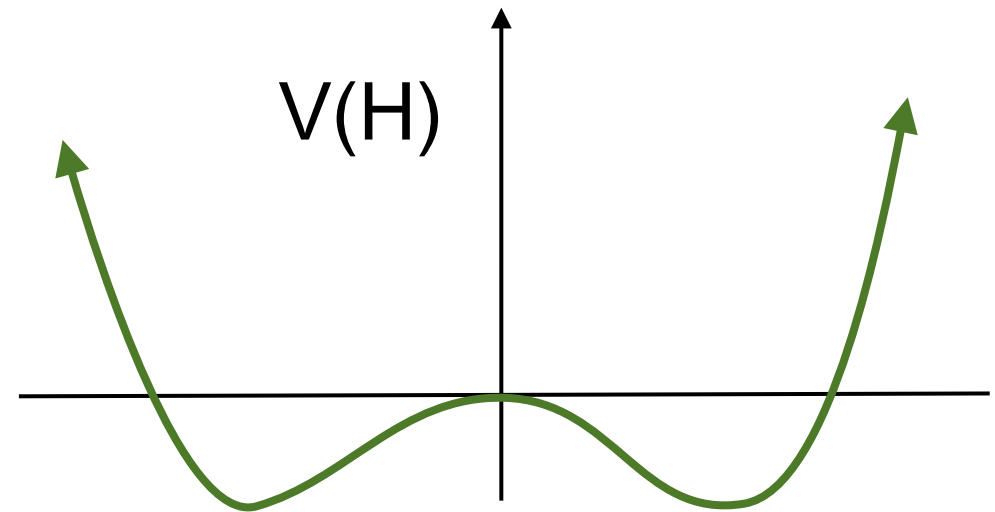
Composite Higgs

at tree-level:



loop-level:

induced by interactions
that explicitly break G
(gauge, Yukawa)



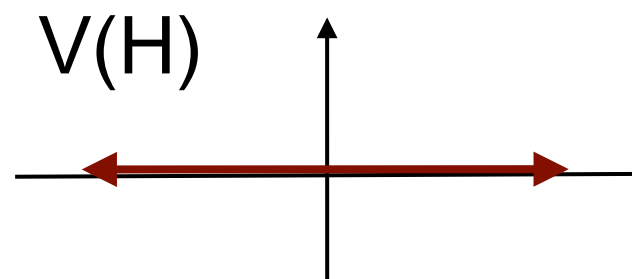
$v \neq 0 \rightarrow$ EWSB
new scale generated

- need $v \neq 0$, but also $v \ll f$

- $m_H^2 = \left. \frac{d^2 V(h)}{d^2 h} \right|_{h=v}$ Higgs mass also needs to be small

Composite Higgs

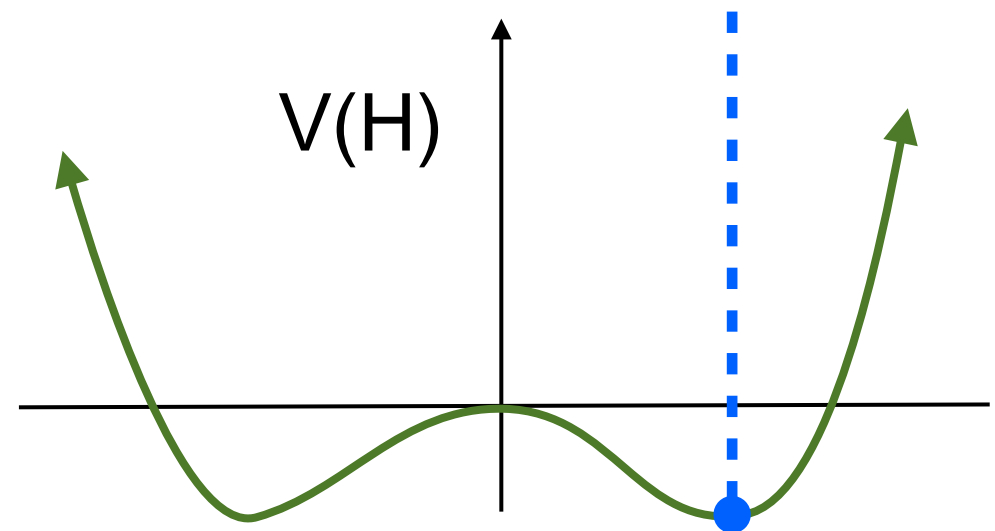
at tree-level:



EWS unbroken

loop-level:

induced by interactions
that explicitly break G
(gauge, Yukawa)



$v \neq 0 \rightarrow$ EWSB

new scale generated

- need $v \neq 0$, but also $v \ll f$

- $m_H^2 = \left. \frac{d^2 V(h)}{d^2 h} \right|_{h=v}$ Higgs mass also needs to be small

Composite Higgs in action

$$\frac{SO(5)}{SO(4)} : \begin{array}{l} 10 \text{ generators} \rightarrow 6 \text{ generators} \\ = 4 \text{ broken generators} = 4 \text{ NGB} \end{array} \quad \text{just enough!}$$

phenomenologically, $G' \supset SU(2) \otimes SU(2) \cong SO(4)$ works better than just $SU(2) \otimes U(1)$... (T parameter)

assemble:

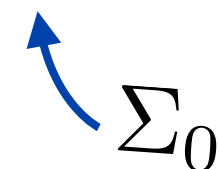
$$\Sigma = \exp \left(\frac{2i \chi_a T^a}{f} \right) \Sigma_0$$

Diagram labels and arrows:
- **strong scale** points to f
- **broken generator** points to T^a
- **NGB** points to the exponent $\frac{2i \chi_a T^a}{f}$
- **symmetry-breaking 'vev'** points to Σ_0

start writing terms with Σ , $D_\mu \Sigma$...

Composite Higgs in action

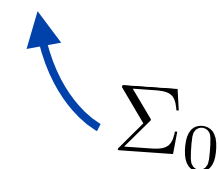
use $SU(3)/(SU(2) \otimes U(1))$ as an explicit example:

$$\Sigma_{ex} = \exp \left\{ \frac{i}{f} \begin{pmatrix} & \chi_4 - i\chi_5 \\ & \chi_6 - i\chi_7 \\ \chi_4 + i\chi_5 & \chi_6 + i\chi_7 \end{pmatrix} \right\} \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}$$


Σ_0

Composite Higgs in action

use $SU(3)/(SU(2) \otimes U(1))$ as an explicit example:

$$\Sigma_{ex} = \exp \left\{ \frac{i}{f} \begin{pmatrix} \boxed{} & \chi_4 - i\chi_5 \\ \chi_4 + i\chi_5 & \chi_6 + i\chi_7 \\ \chi_6 - i\chi_7 & \boxed{} \end{pmatrix} \right\} \begin{pmatrix} \boxed{0} \\ \boxed{0} \\ 1 \end{pmatrix}$$



Σ_0

$SU(2) \otimes U(1)$ correspond to these (unbroken) generators

Composite Higgs in action

use $SU(3)/(SU(2) \otimes U(1))$ as an explicit example:

$$\Sigma_{ex} = \exp \left\{ \frac{i}{f} \begin{pmatrix} \text{Green Box} & \begin{matrix} \chi_4 - i\chi_5 \\ \chi_6 - i\chi_7 \end{matrix} \\ \begin{matrix} \chi_4 + i\chi_5 & \chi_6 + i\chi_7 \end{matrix} & \text{Green Box} \end{pmatrix} \right\} \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}$$


 Σ_0

$SU(2) \otimes U(1)$ correspond to these (unbroken) generators


NGB come with broken generators.

The set of 4: $\chi_{4,5,6,7}$ form a doublet under the $SU(2)_w \otimes U(1)_Y$

Composite Higgs in action

use $SU(3)/(SU(2) \otimes U(1))$ as an explicit example:

$$\Sigma_{ex} = \exp \left\{ \frac{i}{f} \begin{pmatrix} \text{Green Box} & \begin{matrix} \chi_4 - i\chi_5 \\ \chi_6 - i\chi_7 \end{matrix} \\ \begin{matrix} \chi_4 + i\chi_5 & \chi_6 + i\chi_7 \end{matrix} & \text{Green Box} \end{pmatrix} \right\} \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}$$


 Σ_0

$SU(2) \otimes U(1)$ correspond to these (unbroken) generators

NGB come with broken generators.

The set of 4: $\chi_{4,5,6,7}$ form a doublet under the $SU(2)_w \otimes U(1)_Y$

$$\mathcal{L}_\Sigma = \frac{f^2}{4} \text{tr}(D^\mu \Sigma_{ex} D_\mu \Sigma_{ex}^\dagger) + \dots$$

contains interactions of $\chi_{4,5,6,7}$ with
W/Z/ γ and each other

Composite Higgs in action

Now for the real thing: $SO(5)/SO(4)$

$$\mathcal{L}_\Sigma = \frac{f^2}{4} \text{tr}(D^\mu \Sigma D_\mu \Sigma^T) + \dots$$

expand, do lots of algebra...

$$\mathcal{L}_\Sigma = \frac{(\partial_\mu h)^2}{2} + \frac{g^2 f^2}{4} \sin^2 \left(\frac{h}{f} \right) W_\mu^+ W^{-\mu} + \frac{g^2 f^2}{8 \cos^2 \theta} \sin^2 \left(\frac{h}{f} \right) Z_\mu^0 Z^{0\mu}$$

Composite Higgs in action

Now for the real thing: SO(5)/SO(4)

$$\mathcal{L}_\Sigma = \frac{f^2}{4} \text{tr}(D^\mu \Sigma D_\mu \Sigma^T) + \dots$$

expand, do lots of algebra...

$$\mathcal{L}_\Sigma = \frac{(\partial_\mu h)^2}{2} + \frac{g^2 f^2}{4} \sin^2 \left(\frac{h}{f} \right) W_\mu^+ W^{-\mu} + \frac{g^2 f^2}{8 \cos^2 \theta} \sin^2 \left(\frac{h}{f} \right) Z_\mu^0 Z^{0\mu}$$

ASSUMING: $\langle h \rangle \neq 0$ (have to justify later with $V(h)$)

set $h \rightarrow h + \langle h \rangle$ in above, and expand

define: $v = f \sin \left(\frac{\langle h \rangle}{f} \right)$

EW scale v < scale of
strong dynamics f

Composite Higgs in action

Now for the real thing: SO(5)/SO(4)

$$\mathcal{L}_\Sigma = \frac{f^2}{4} \text{tr}(D^\mu \Sigma D_\mu \Sigma^T) + \dots \quad ???$$

expand, do lots of algebra...

$$\mathcal{L}_\Sigma = \frac{(\partial_\mu h)^2}{2} + \frac{g^2 f^2}{4} \sin^2 \left(\frac{h}{f} \right) W_\mu^+ W^{-\mu} + \frac{g^2 f^2}{8 \cos^2 \theta} \sin^2 \left(\frac{h}{f} \right) Z_\mu^0 Z^{0\mu}$$

ASSUMING: $\langle h \rangle \neq 0$ (have to justify later with $V(h)$)

set $h \rightarrow h + \langle h \rangle$ in above, and expand

define: $v = f \sin \left(\frac{\langle h \rangle}{f} \right)$

EW scale v < scale of
strong dynamics f

Composite Higgs in action

Keep expanding: $\frac{g^2 f^2}{4} \sin^2 \left(\frac{h}{f} \right) W_\mu^+ W^{-\mu}$

$$f^2 \sin^2 \left(\frac{h}{f} \right) = v^2 + 2 v h \sqrt{1 - \xi} + h^2 (1 - 2\xi) + \dots$$

where: $\xi = \frac{v^2}{f^2}$

reshuffling things... $m_W^2 \left(1 + a \frac{2h}{v} + b \frac{h^2}{v^2} + \dots \right)$

\therefore in the SO(5)/SO(4) composite Higgs model

$$a = \sqrt{1 - \frac{v^2}{f^2}} \quad , \quad b = 1 - 2 \frac{v^2}{f^2}$$

Higgs couplings deviate from SM values

Composite Higgs in action

$a \neq 1$: eventual bad behavior in $W_L W_L \rightarrow W_L W_L$ amplitudes

at $\frac{4\sqrt{\pi}v}{\sqrt{1-a}} \sim 4\sqrt{\pi}v \frac{f^2}{v^2}$

eventual strong dynamics...
 \therefore expect **resonances** at scale
 $\sim f$ in analogy with to QCD
 $\rho', a', \omega', \text{etc.}$

want strong coupling scale pushed to \sim few TeV (at least)

other patterns of symmetry breaking would have different values for
 a, b , as well as more states

ex.) $SO(6)/SO(5)$ has 5 NGBs,
 $4 \in H + 1$ extra scalar η

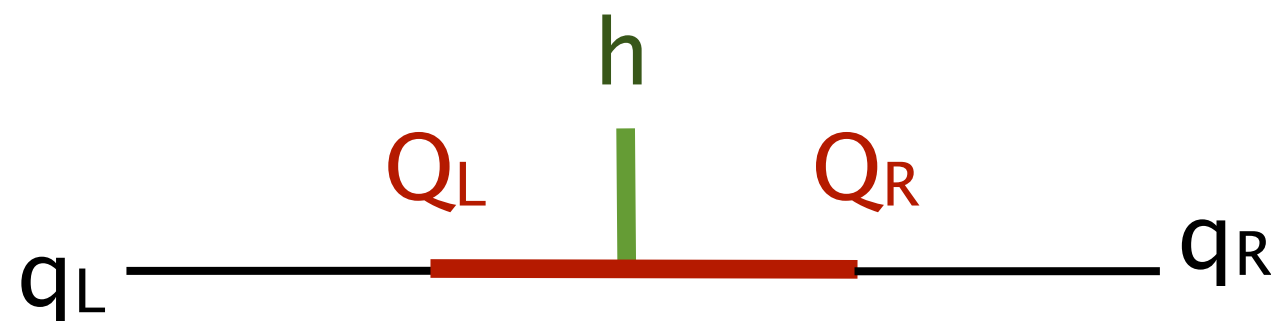
many other
possibilities

Partial Compositeness

How do fermions get mass?

they mix with composite fermions \sim **baryons of the new strong interaction**

- composite baryons are massive even without EWSB, just as proton would have mass even without quark masses.
- proton interacts strongly with QCD pion \therefore composite fermions will interact strongly with composite higgs.

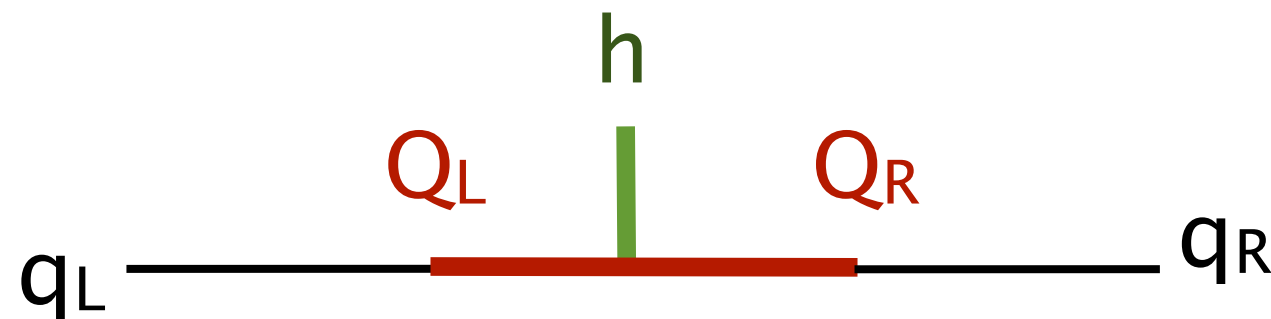


Partial Compositeness

How do fermions get mass?

they mix with composite fermions \sim **baryons of the new strong interaction**

- composite baryons are massive even without EWSB, just as proton would have mass even without quark masses.
- proton interacts strongly with QCD pion \therefore composite fermions will interact strongly with composite higgs.



- the price we pay is new states, the composite fermions..
new states \rightarrow new LHC signals

Partial Compositeness

in practice:

$$\mathcal{L}_F = \Delta_L Q_L \mathcal{Q}_R + \Delta_R t_R \mathcal{T}_L + \mathcal{M}_Q \mathcal{Q}_L \mathcal{Q}_R + \mathcal{M}_T \mathcal{T}_L \mathcal{T}_R + Y_T \mathcal{Q}_L \Sigma \mathcal{T}_R + h.c.$$

Diagram annotations:

- Arrows from "composite fermions" point to \mathcal{Q}_R and \mathcal{T}_L .
- Arrows from "mass terms for composites" point to $\mathcal{M}_Q \mathcal{Q}_L \mathcal{Q}_R$ and $\mathcal{M}_T \mathcal{T}_L \mathcal{T}_R$.
- An arrow from "SM fields" points to Q_L and t_R .
- An arrow from "composite + higgs couplings" points to $Y_T \mathcal{Q}_L \Sigma \mathcal{T}_R$.

Undo the mixing:

$$\begin{aligned} \mathcal{Q}_L &= \cos(\phi_L) \mathcal{Q}_H + \sin(\phi_L) q_L \\ Q_L &= -\sin(\phi_L) \mathcal{Q}_H + \cos(\phi_L) q_L \\ &\quad + \text{similar for } t_R \mathcal{T}_{L,R} \end{aligned}$$

yields $(q_L h t_R^*) Y_T \sin(\phi_L) \sin(\phi_R)$

Partial Compositeness

in practice:

$$\mathcal{L}_F = \Delta_L Q_L \mathcal{Q}_R + \Delta_R t_R \mathcal{T}_L + \mathcal{M}_Q \mathcal{Q}_L \mathcal{Q}_R + \mathcal{M}_T \mathcal{T}_L \mathcal{T}_R + Y_T \mathcal{Q}_L \Sigma \mathcal{T}_R + h.c.$$

Diagram annotations:

- Arrows from "composite fermions" point to \mathcal{Q}_R and \mathcal{T}_L .
- Arrows from "mass terms for composites" point to $\mathcal{M}_Q \mathcal{Q}_L \mathcal{Q}_R$ and $\mathcal{M}_T \mathcal{T}_L \mathcal{T}_R$.
- An arrow from "SM fields" points to Q_L and t_R .
- An arrow from "composite + higgs couplings" points to $Y_T \mathcal{Q}_L \Sigma \mathcal{T}_R$.

Undo the mixing:

$$\begin{aligned} \mathcal{Q}_L &= \cos(\phi_L) \mathcal{Q}_H + \sin(\phi_L) q_L \\ Q_L &= -\sin(\phi_L) \mathcal{Q}_H + \cos(\phi_L) q_L \\ &\quad + \text{similar for } t_R \mathcal{T}_{L,R} \end{aligned}$$

yields $(q_L h t_R^*) Y_T \sin(\phi_L) \sin(\phi_R)$ exact form depends on how composites transform under G

Partial Compositeness

in practice:

$$\text{different from } y f Q_L \Sigma u_R^* \rightarrow y \frac{(Q_L u_R^*)(\bar{\psi}\psi)}{\Lambda^2}$$

$$\mathcal{L}_F = \Delta_L Q_L \mathcal{Q}_R + \Delta_R t_R \mathcal{T}_L + \mathcal{M}_Q \mathcal{Q}_L \mathcal{Q}_R + \mathcal{M}_T \mathcal{T}_L \mathcal{T}_R + Y_T \mathcal{Q}_L \Sigma \mathcal{T}_R + h.c.$$

Diagram annotations:

- Arrows from "composite fermions" point to \mathcal{Q}_R and \mathcal{T}_L .
- Arrows from "mass terms for composites" point to $\mathcal{M}_Q \mathcal{Q}_L \mathcal{Q}_R$ and $\mathcal{M}_T \mathcal{T}_L \mathcal{T}_R$.
- An arrow from "SM fields" points to Q_L and t_R .
- An arrow from "composite + higgs couplings" points to $Y_T \mathcal{Q}_L \Sigma \mathcal{T}_R$.

Undo the mixing:

$$\begin{aligned} \mathcal{Q}_L &= \cos(\phi_L) \mathcal{Q}_H + \sin(\phi_L) q_L \\ Q_L &= -\sin(\phi_L) \mathcal{Q}_H + \cos(\phi_L) q_L \\ &\quad + \text{similar for } t_R \mathcal{T}_{L,R} \end{aligned}$$

yields $(q_L h t_R^*) Y_T \sin(\phi_L) \sin(\phi_R)$ exact form depends on how composites transform under G

Recap:

Composite Higgs models are characterized by two scales: f and v

- Higgs couplings deviate from SM values at $O(v^2/f^2)$

i.e. for $SO(5)/SO(4)$ “MCHM”

$$\frac{g_{hVV}}{g_{hVV,SM}} = \sqrt{1 - \frac{v^2}{f^2}}, \quad \frac{g_{hhVV}}{g_{hhVV,SM}} = 1 - 2\frac{v^2}{f^2}, \quad \frac{g_{t\bar{t}h}}{g_{t\bar{t}h,SM}} = \sqrt{1 - \frac{v^2}{f^2}}$$

set by G/G' pattern

set by composite fermion rep.

- new dynamics at f , new states at $O(f-4\pi f)$

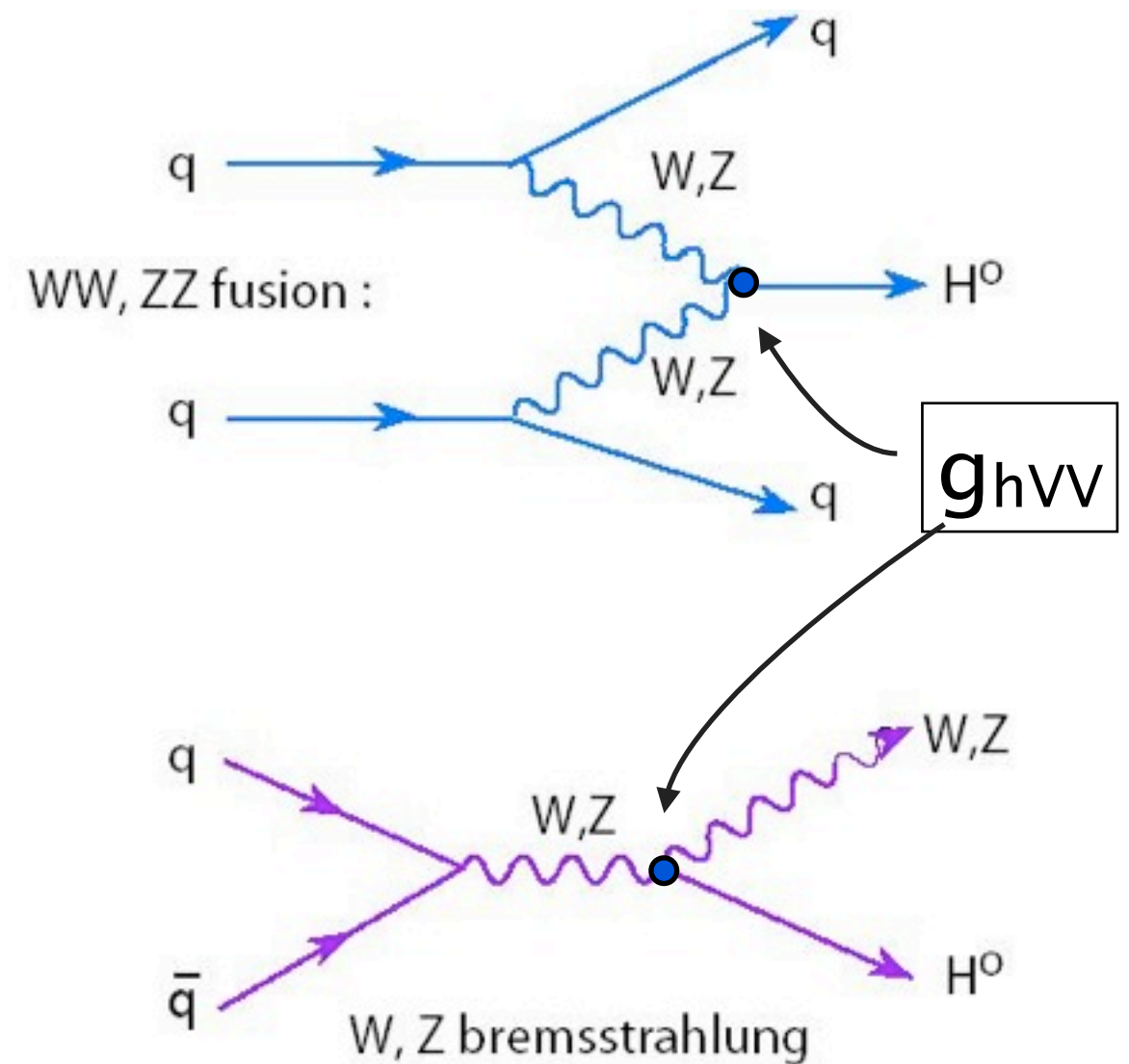
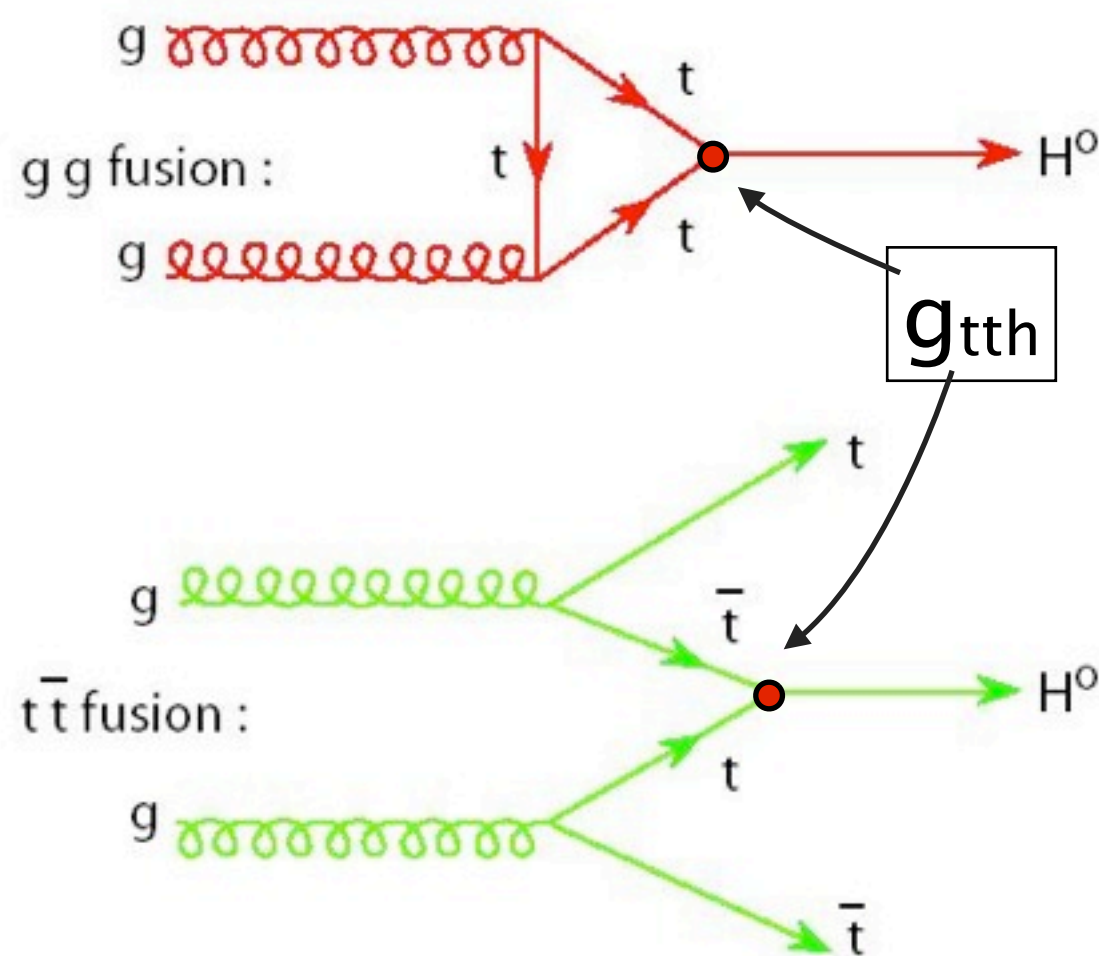
new spin-1 resonances: ρ' , a' , etc.

new spin-1/2 resonances: composite fermions

LHC signals: Higgs couplings

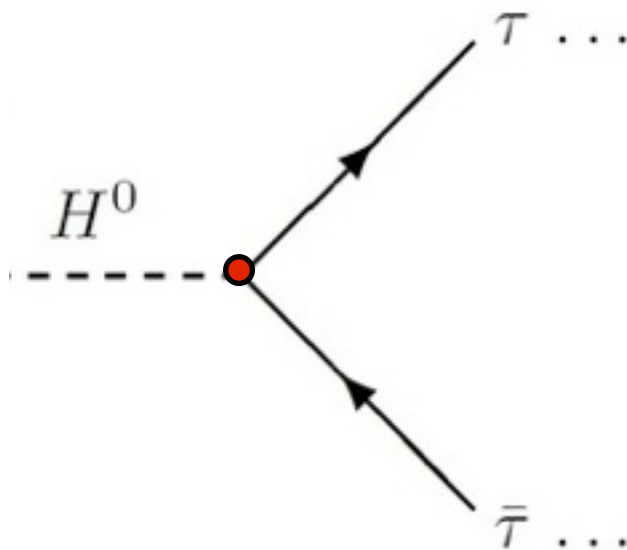
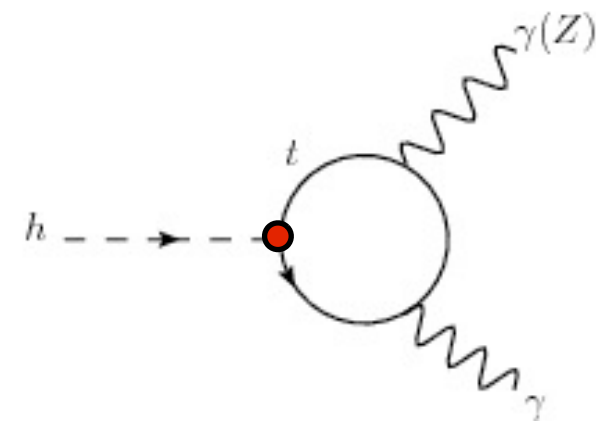
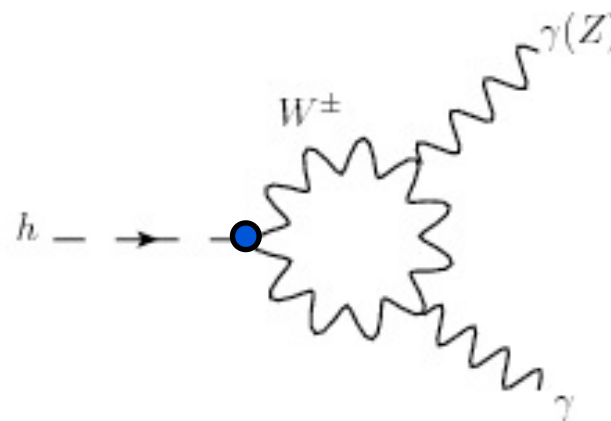
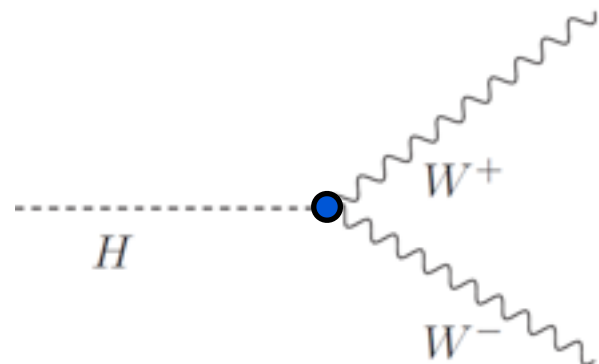
study all possible Higgs production and decay process to extract g_{hVV} , g_{tth}

intricate process, as different production mechanisms scale differently with g_{hVV} , g_{tth} and contribute differently to each final state



LHC signals: Higgs couplings

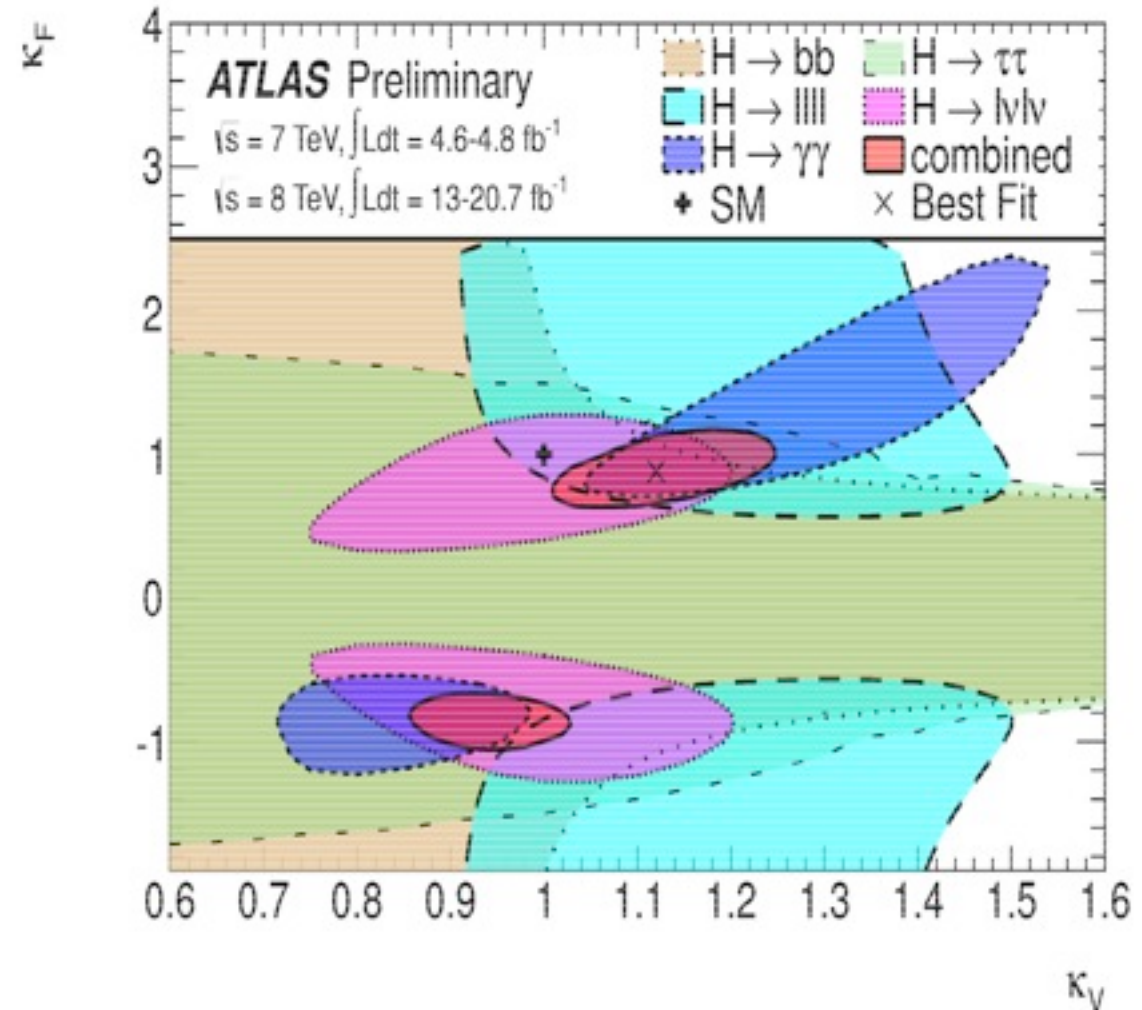
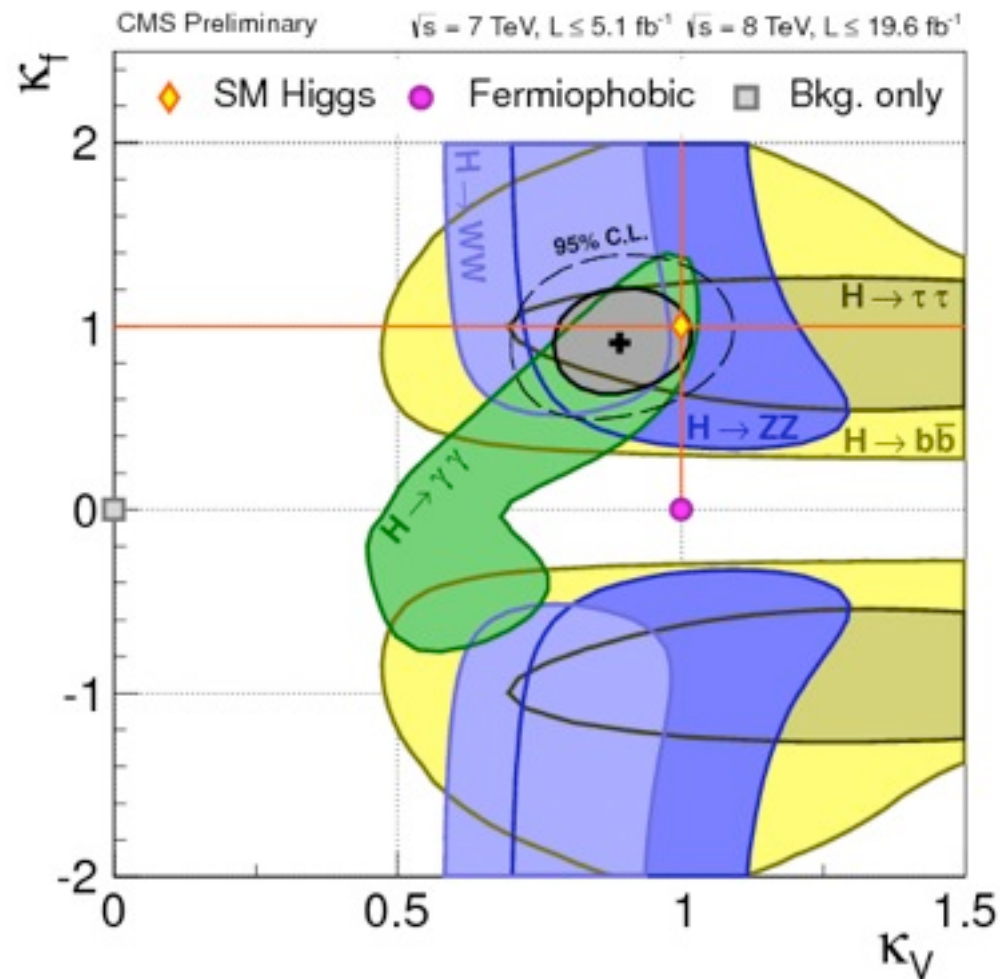
different composite Higgs models \rightarrow different g_{hVV} , g_{htt} , possibly even extra Higgs decay modes from new particles



ex.) $gg \rightarrow h \rightarrow W_{\mu}^{+} W_{\mu}^{-} \sim g_{hVV} g_{tth}/\Gamma_H$
 $VBF \text{ } pp \rightarrow h \rightarrow \tau^{+} \tau^{-} \sim g_{hVV} g_{\tau\tau h}/\Gamma_H$
 $gg \rightarrow h \rightarrow \tau^{+} \tau^{-} \sim g_{tth} g_{\tau\tau h}/\Gamma_H$

BUT, careful: $H + jj$ is not VBF alone, $H+0j$ is not just $gg \rightarrow H$
also, Γ_H knows about all g_{ffh}

LHC signals: Higgs couplings



both LHC expts. already cast results in space of

$$\kappa_V = \frac{g_{hVV}}{g_{hVV,SM}}, \quad \kappa_f = \frac{g_{t\bar{t}h}}{g_{t\bar{t}h,SM}}$$

roughly, $|\kappa_V - 1| \lesssim 0.2$, $v \gtrsim 550 \text{ GeV}$ (though caveats remain)

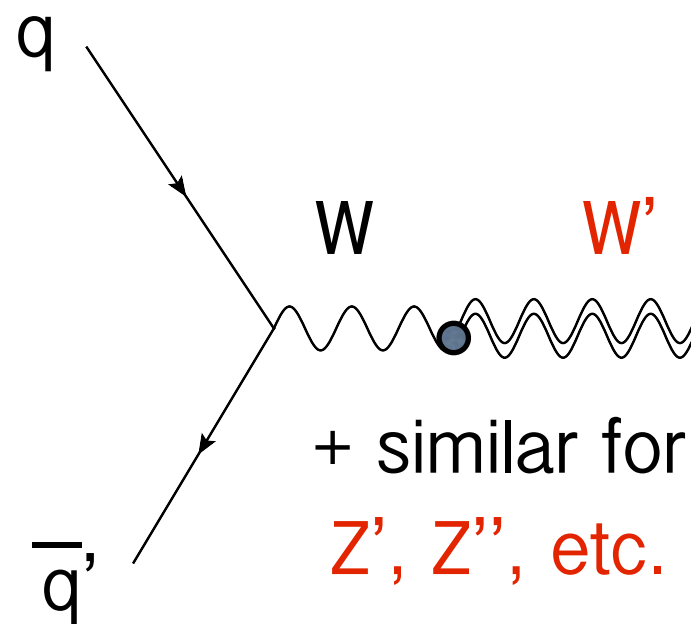
improvements? $|\kappa_V - 1| \approx 0.1$ possible...

hard to get much better due to uncertainties (PDF/ σ_h /vetoes)!

LHC signals: spin-1 resonances

slight mixing between W' , Z' and W , Z , means new resonances
produced most easily in \hat{s} -channel

may look like usual W' , Z'



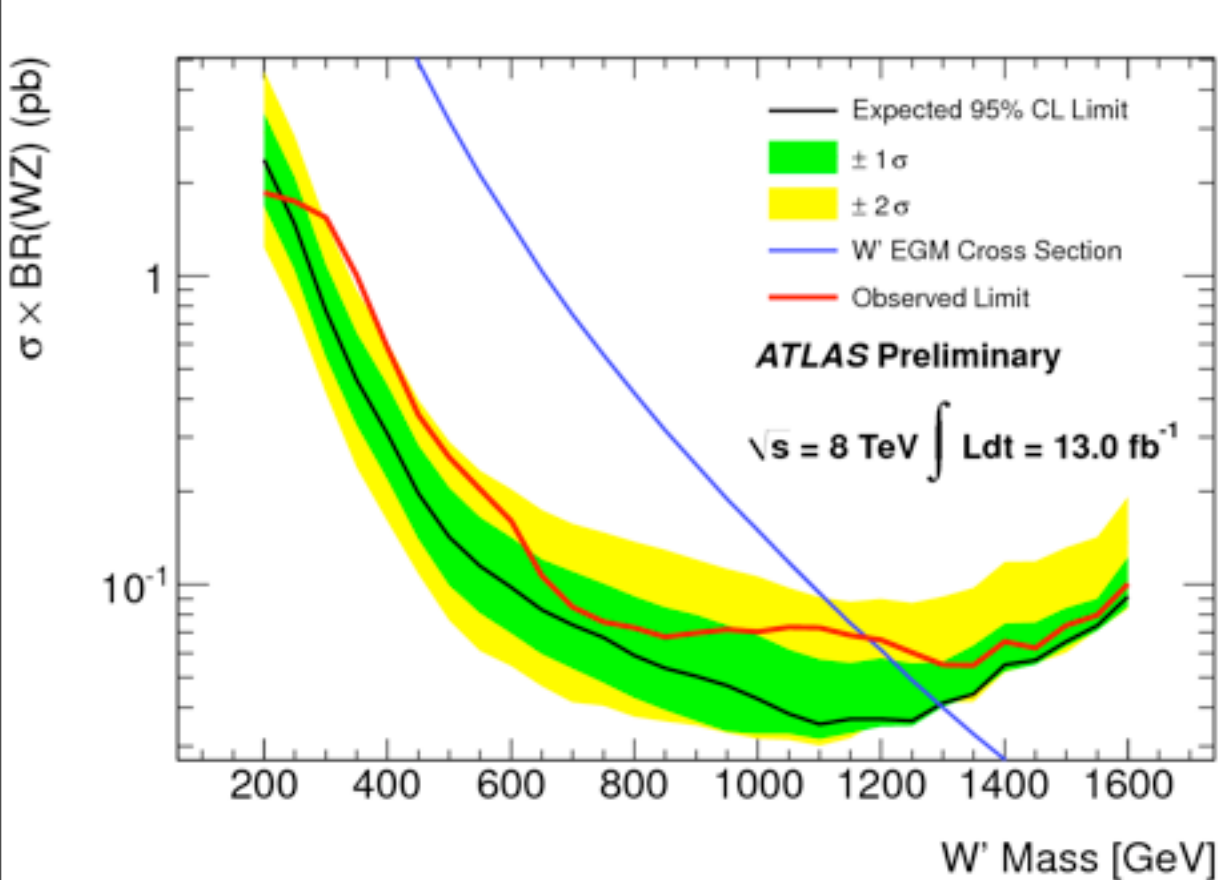
BUT: W' , Z' couple strongest to other
strong-sector states, like the
longitudinal
 W , Z & h (even t). Big couplings mean
 $\Gamma_{W'}$, etc. can be big.

usual W' , Z' LHC searches assume zero (or very small)
 $W'WZ$ interactions... these **need to be reinterpreted** for
particles w/ strong interactions with W , Z , etc.

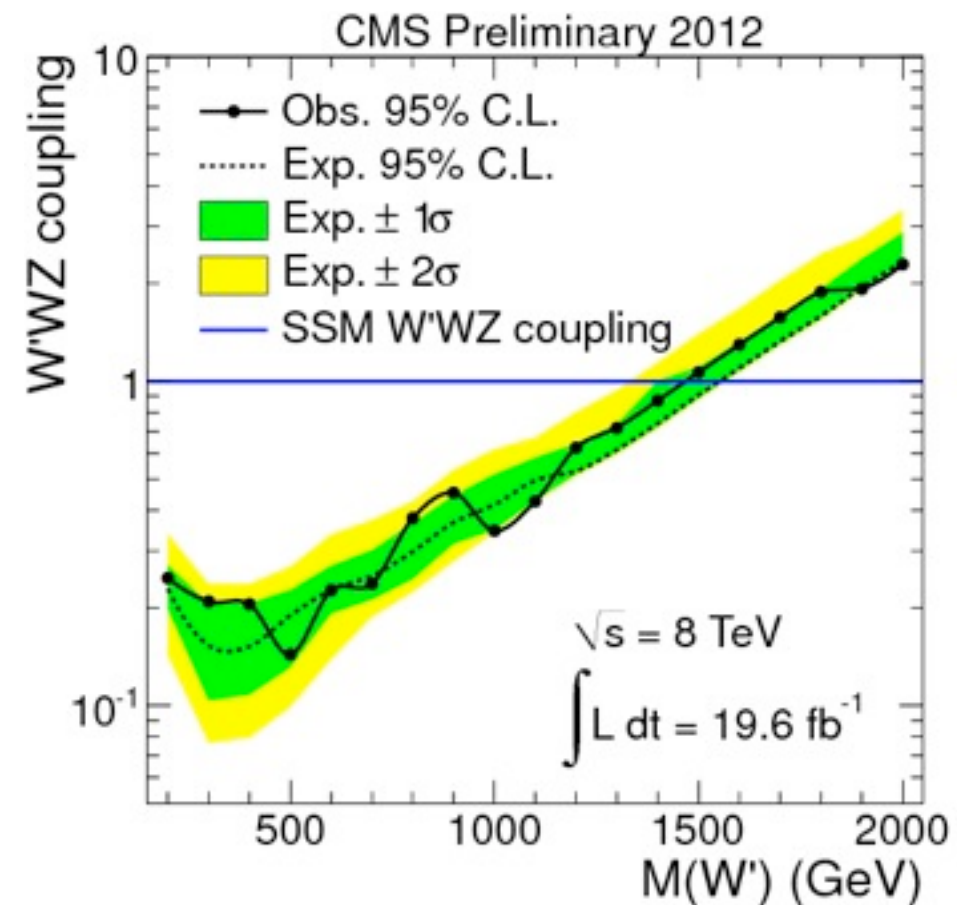
LHC signals: spin-1 resonances

cleanest signal for W/Z decay products is the fully leptonic mode:

$$W' \rightarrow WZ \rightarrow 3\ell + \nu$$



ATLAS 13.0 fb⁻¹



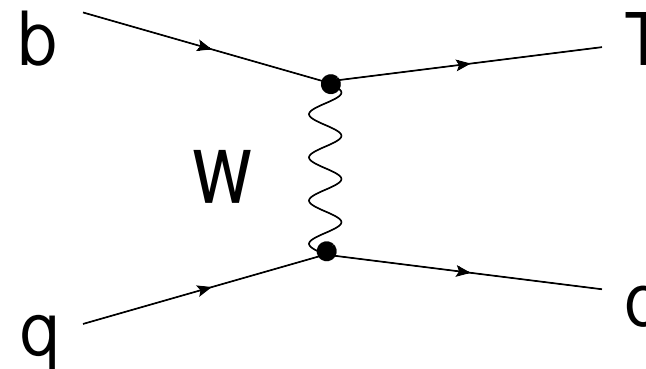
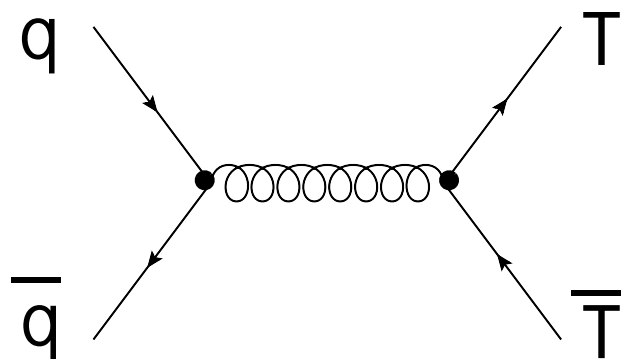
CMS 19.6 fb⁻¹

existing studies assume small W'WZ coupling!

leptonic modes have small BR .. combined with small production cross section, rate will be a problem as $m_{W'}$ increases

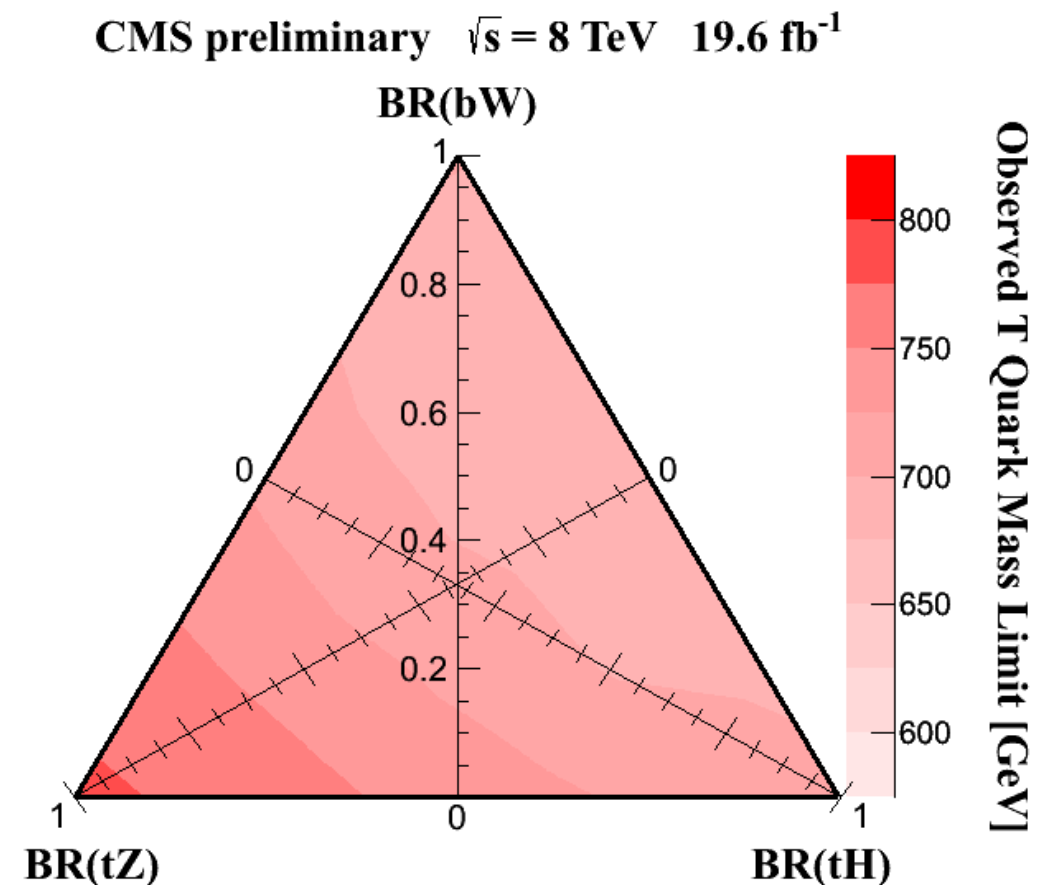
LHC signals: fermionic resonances

top/bottom-partners usually lightest new fermions
can be pair- or singly-produced



often decay to $W/Z/H + t/b...$
exact modes, BR depend on the
model

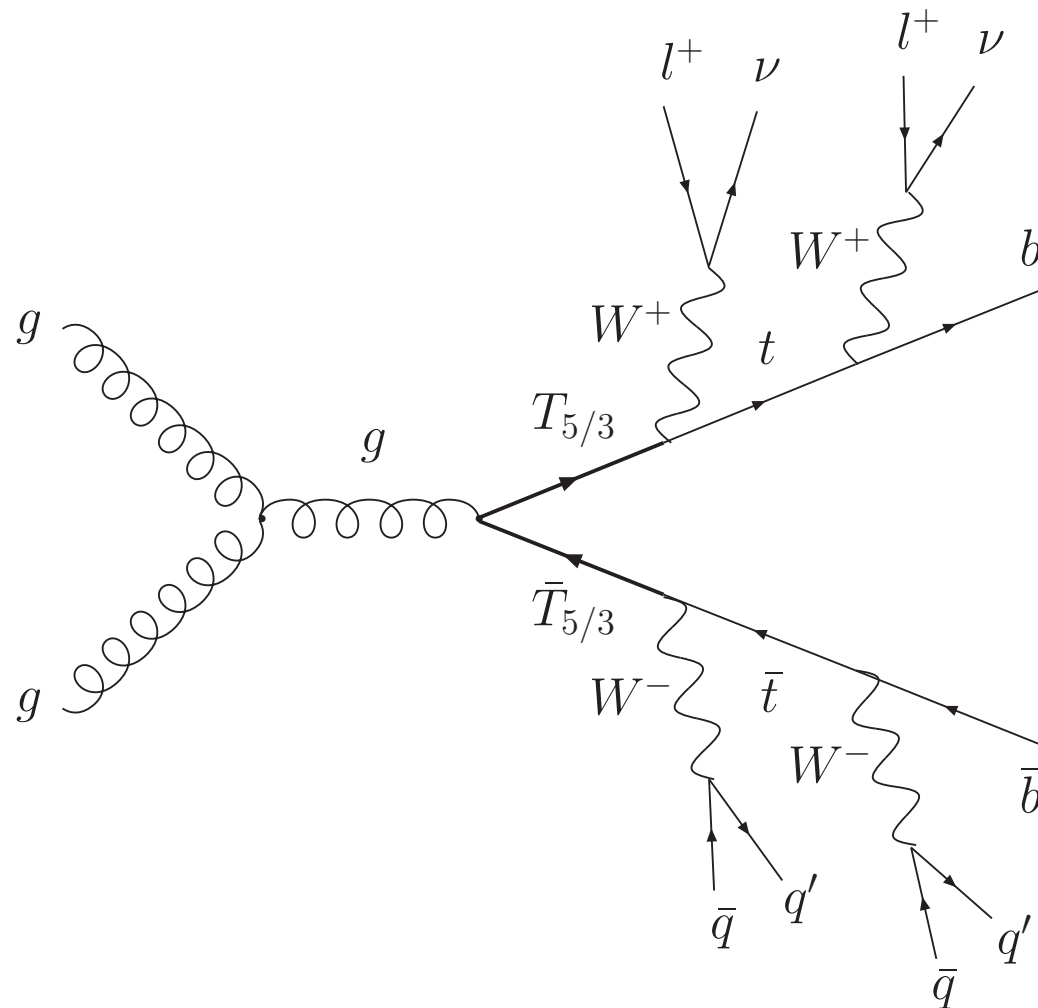
[CMS B2G-12-015,
ATLAS-CONF-2013-056, -058, -018]



LHC signals: fermionic resonances

stronger bounds from exotically charged new fermions

t_L partner \sim part of larger SU(2) rep.
containing $X_{5/3}$ (helps w/ $Zb\bar{b}$)



pair-production of $X_{5/3}$
generates SSL signal

very little SM background
 \rightarrow strong limit

$$m_X \gtrsim 770 \text{ GeV}$$

[CMS PAS B2G-12-012,
ATLAS-CONF-2013-051]

limit pulls up mass of whole multiplet

about that Higgs potential...

new f-scale dynamics impact Higgs through potential (v , m^2_H)

rewrite \mathcal{L}_{CH}
differently...

$$\mathcal{L} = \frac{1}{2} (P_T)^{\mu\nu} \left[\left(\Pi_0^X(q^2) + \Pi_0(q^2) + \frac{\sin^2(h/f)}{4} \Pi_1(q^2) \right) B_\mu B_\nu \right. \\ \left. + \left(\Pi_0(q^2) + \frac{\sin^2(h/f)}{4} \Pi_1(q^2) \right) A_\mu^{a_L} A_\nu^{a_L} \right. \\ \left. + 2 \sin^2(h/f) \Pi_1(q^2) \hat{H}^\dagger T^{a_L} Y \hat{H} A_\mu^{a_L} B_\nu \right],$$

form factors Π_0 , Π_1 encapsulate strong dynamics

about that Higgs potential...

new f-scale dynamics impact Higgs through potential (v , m^2_H)

rewrite \mathcal{L}_{CH}
differently...

$$\mathcal{L} = \frac{1}{2}(P_T)^{\mu\nu} \left[\left(\Pi_0^X(q^2) + \Pi_0(q^2) + \frac{\sin^2(h/f)}{4} \Pi_1(q^2) \right) B_\mu B_\nu \right. \\ \left. + \left(\Pi_0(q^2) + \frac{\sin^2(h/f)}{4} \Pi_1(q^2) \right) A_\mu^{a_L} A_\nu^{a_L} \right. \\ \left. + 2 \sin^2(h/f) \Pi_1(q^2) \hat{H}^\dagger T^{a_L} Y \hat{H} A_\mu^{a_L} B_\nu \right],$$

form factors Π_0 , Π_1 encapsulate strong dynamics

$$\langle J_\mu^a(q) J_\nu^a(-q) \rangle = \Pi_0(q^2) (P_T)_{\mu\nu} \quad \text{2-pt function of unbroken (SO(4)) currents}$$

$$\langle J_\mu^a(q) J_\nu^a(-q) \rangle - \langle J_\mu^{\hat{a}}(q) J_\nu^{\hat{a}}(-q) \rangle = -\frac{1}{2} \Pi_1(q^2) (P_T)_{\mu\nu} \\ \text{difference of unbroken-broken currents}$$

about that Higgs potential...

new f-scale dynamics impact Higgs through potential (v , m^2_H)

rewrite \mathcal{L}_{CH}
differently...

$$\mathcal{L} = \frac{1}{2} (P_T)^{\mu\nu} \left[\left(\Pi_0^X(q^2) + \Pi_0(q^2) + \frac{\sin^2(h/f)}{4} \Pi_1(q^2) \right) B_\mu B_\nu \right. \\ \left. + \left(\Pi_0(q^2) + \frac{\sin^2(h/f)}{4} \Pi_1(q^2) \right) A_\mu^{a_L} A_\nu^{a_L} \right. \\ \left. + 2 \sin^2(h/f) \Pi_1(q^2) \hat{H}^\dagger T^{a_L} Y \hat{H} A_\mu^{a_L} B_\nu \right],$$

form factors Π_0 , Π_1 encapsulate strong dynamics

$$\langle J_\mu^a(q) J_\nu^a(-q) \rangle = \Pi_0(q^2) (P_T)_{\mu\nu} \quad \text{2-pt function of unbroken (SO(4)) currents}$$

$$\langle J_\mu^a(q) J_\nu^a(-q) \rangle - \langle J_\mu^{\hat{a}}(q) J_\nu^{\hat{a}}(-q) \rangle = -\frac{1}{2} \Pi_1(q^2) (P_T)_{\mu\nu} \\ \text{difference of unbroken-broken currents}$$

know some properties of Π_0 , Π_1 at $q^2 = 0, \infty$

$$\text{i.e. } \Pi_0(0) = 0, \Pi_1(0) = f^2$$

but general structure unknown

about that Higgs potential...

$$S \propto \Pi'_1(0)$$

new f-scale dynamics impact Higgs through potential (v , m^2_H)

rewrite \mathcal{L}_{CH}
differently...

$$\mathcal{L} = \frac{1}{2}(P_T)^{\mu\nu} \left[\left(\Pi_0^X(q^2) + \Pi_0(q^2) + \frac{\sin^2(h/f)}{4} \Pi_1(q^2) \right) B_\mu B_\nu \right. \\ \left. + \left(\Pi_0(q^2) + \frac{\sin^2(h/f)}{4} \Pi_1(q^2) \right) A_\mu^{a_L} A_\nu^{a_L} \right. \\ \left. + 2 \sin^2(h/f) \Pi_1(q^2) \hat{H}^\dagger T^{a_L} Y \hat{H} A_\mu^{a_L} B_\nu \right],$$

form factors Π_0 , Π_1 encapsulate strong dynamics

$$\langle J_\mu^a(q) J_\nu^a(-q) \rangle = \Pi_0(q^2) (P_T)_{\mu\nu} \quad \text{2-pt function of unbroken (SO(4)) currents}$$

$$\langle J_\mu^a(q) J_\nu^a(-q) \rangle - \langle J_\mu^{\hat{a}}(q) J_\nu^{\hat{a}}(-q) \rangle = -\frac{1}{2} \Pi_1(q^2) (P_T)_{\mu\nu} \\ \text{difference of unbroken-broken currents}$$

know some properties of Π_0 , Π_1 at $q^2 = 0, \infty$

$$\text{i.e. } \Pi_0(0) = 0, \Pi_1(0) = f^2$$

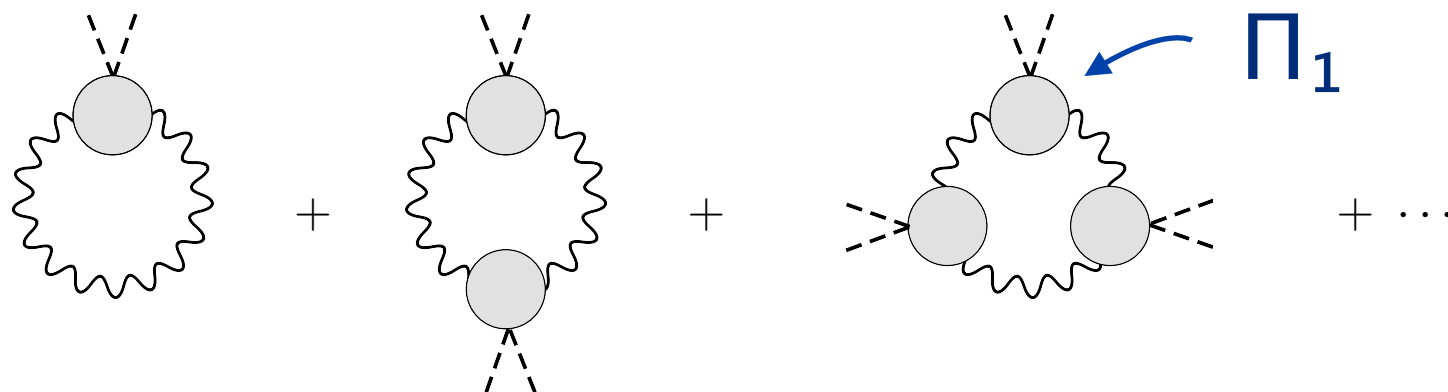
but general structure unknown

about that Higgs potential...

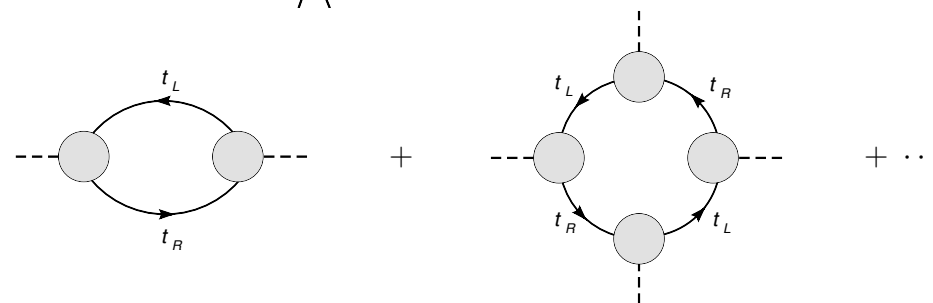
similarly, in
fermion sector

$$\begin{aligned}\mathcal{L} = & \bar{q}_L \not{p} \left(\Pi_0^q(p) + \Pi_1^q(p) \cos(h/f) \right) q_L \\ & + \bar{t}_R \not{p} \left(\Pi_0^u(p) - \Pi_1^u(p) \cos(h/f) \right) t_R \\ & + \sin(h/f) M_1^u(p) \bar{q}_L \hat{H}^c t_R + h.c.\end{aligned}$$

form $V(H)$ by resumming...



analogous to $\pi^\pm - \pi^0$ mass
difference in QCD...



but for a different χ SB pattern,
different underlying strong dynamics

about that Higgs potential...

without really knowing Π_i , etc. model-builders resort to

large- N_c vector-meson-dominance

“AdS/CFT”-inspired extra-dimensions

NDA

important since Π_i modeling ties new resonances to $V(h)$ and
thereby to EWSB and m_h^2

$$m_h^2 = 2N_c \frac{y_t^2}{8\pi^2} m_*^2 \xi \quad , \quad \xi = \frac{v^2}{f^2}, \quad m^* = \kappa m_T \quad \text{modeling}$$

about that Higgs potential...

without really knowing Π_i , etc. model-builders resort to

large- N_c vector-meson-dominance

“AdS/CFT”-inspired extra-dimensions

NDA

do give proof-of-principle, calculable
example.. but getting tuned

important since Π_i modeling ties new resonances to $V(h)$ and
thereby to EWSB and m_h^2

$$m_h^2 = 2N_c \frac{y_t^2}{8\pi^2} m_*^2 \xi \quad , \quad \xi = \frac{v^2}{f^2}, \quad m^* = \kappa m_T \quad \text{modeling}$$

about that Higgs potential...

without really knowing Π_i , etc. model-builders resort to

large- N_c

vector-meson-dominance

“AdS/CFT”-inspired extra-dimensions

NDA

do give proof-of-principle, calculable example.. but getting tuned

important since Π_i modeling ties new resonances to $V(h)$ and thereby to EWSB and m_h^2

$$m_h^2 = 2N_c \frac{y_t^2}{8\pi^2} m_*^2 \xi, \quad \xi = \frac{v^2}{f^2}, \quad m^* = \kappa m_T$$

modeling

but are these assumptions any good? generic?

help from the lattice!

about that Higgs potential...

big questions for composite Higgs after 20 fb^{-1} LHC data:

- can we get $v, m_h \ll m_{W'}, m_T$ in CH setup?
- what are the properties of those theories?

about that Higgs potential...

big questions for composite Higgs after 20 fb^{-1} LHC data:

- can we get $v, m_h \ll m_{W'}, m_T$ in CH setup?
- what are the properties of those theories?

lattice input in these theories could really help:

spectrum (pNGB, spin-1, spin-1/2 resonances),
 L_X/OPE coefficients, $\Pi_i(q^2)$ etc. = shape of potential

about that Higgs potential...

big questions for composite Higgs after 20 fb^{-1} LHC data:

- can we get $v, m_h \ll m_{W'}, m_T$ in CH setup?
- what are the properties of those theories?

lattice input in these theories could really help:

spectrum (pNGB, spin-1, spin-1/2 resonances),
 L_χ/OPE coefficients, $\Pi_i(q^2)$ etc. = shape of potential

know from $SU(N)^2/SU(N)$ lattice studies that different N_F ,
representation, etc. lead to behavior different from vanilla QCD.

what happens with different χ SB pattern?

conclusions

composite Higgs = Higgs as a pNGB, formed
from new strong dynamics at f

gauge and Yukawa interactions generate nontrivial $V(h)$ and
lead to EWSB. tuning of different contributions to get $v \ll f$

$O(v^2/f^2)$ Higgs coupling deviations, new heavy resonances
(spin-1, fermions) in spectra, all targets for LHC searches

resonance \leftrightarrow Higgs interplay requires understanding/
modeling strong dynamics.

lattice insight needed

other directions

new composite sector & Dark Matter:

- lightest `techni'baryon can be stable by analog of $U(1)_B$
- an initial matter/anti-matter asymmetry gets shared among baryons, leptons, `techni'baryons via sphalerons
(Chivukula, Barr, Fahri, Nussinov)
- can get observed Ω_{DM}/Ω_B easily for $\sim \text{TeV}$ scale DM
must be electrically neutral, EW singlets to avoid direct detection
Then leading operators are **charge radius** and **polarizability**:

ex.)
$$\frac{B^* B v_\mu \partial_\nu F^{\mu\nu}}{\Lambda_{TC}^2}, \quad \frac{B^* B F_{\mu\nu} F^{\mu\nu}}{\Lambda_{TC}^3}$$

lattice input?

